

NOISE ANALYSIS OF THE COARSE OPTICAL POWER SPECTRUM ESTIMATOR (COPSE) DATA ACQUISITION SYSTEM

by

by

D.L. Desaulniers
Remote Sensing Section
Electronics Division

DEFENCE RESEARCH ESTABLISHMENT OTTAWA TECHNICAL NOTE 82-8

PCN 33D00 March 1984 Ottawa

ABSTRACT

The various components of the COPSE Acquisition System are briefly summarized. The system is theoretically analysed to determine what effect added Gaussian noise will have on its performance. On linear mode, the Gaussian noise was found to negate the quantization effect of the system provided the variance of the noise was high enough. On log mode, the system was found to perform better in the low photo-diode current range.

RÉSUMÉ

Les divers éléments du système de saisie des données COPSE font d'objet d'une brève description. Le système est analysé du point de vue théorique pour déterminer les effets possibles du bruit gaussien ajouté sur son fonctionnement. En mode linéaire, on a constaté que le bruit gaussien annulait l'effet de quantification du système lorsque la variance du bruit était suffisamment élevée. En mode logarithmique, on a constaté que le système avait un meilleur rendement lorsque la photo-diode avait un faible courant.

Access	ion For		
NTIS DTIC T	GRA&I AB	X	
	ibution/		
•	Avail a Speci	nd/or	

TABLE OF CONTENTS

	<u>PA</u>	GE
ABSTRA	T/RESUME i	ii
TABLE	F CONTENTS	iv
LIST O	ILLUSTRATIONS	٧
TABLE	OF SYMBOLS	vi
1.0	INTRODUCTION	1
2.0	COPSE DATA ACQUISITION SYSTEM	3
3.0	NOISE ANALYSIS	7
	3.1 Linear Mode of Operation	0 4
4.0	REFERENCES 1	9

LIST OF ILLUSTRATIONS

			PAGE
Figure	1:	COPSE System	2
Figure	2:	Plot of $\frac{\Delta V_{I}(k)}{\Delta i_{k} }$ Versus $ i_{k} $ for Both Modes of Operation	5
Figure	3:	COPSE Electronic Subsystem with Noise Added	8
Figure	4:	Estimated Photo-Diode Output Currents for a Collimated Gaussian Beam	11
Figure	5:	Plot of of Versus G-M for Linear Mode of Operation	13
Figure	6:	A) Plot of $\sigma_{n,k}^2$ Versus $\frac{\sigma_k^2}{ f_k ^2}$. 18
		B) Plot of σ_n^2 , Versus ℓ on Log Mode	

on the second of the second second of the second of the

TABLE OF SYMBOLS

```
becomes
          constant
          approximately equal to
          quantization error
\mathbf{e}_{\mathbf{q}}
          quantization error with noise
          sample average of en
E{...}
         expectation value of
G
          gain
          greater than
          output current of k<sup>th</sup> photo-diode
ik
|ik|
          absolute value of ik
|i_k|_e
          calculated estimate of |ik|
\Delta |i_k|
          incremental change in |i,|
          photo-diode element number (k = 1, 2, 3, \ldots, 64)
k
          digital output of A/D converter for kth photo-diode
Lk
          digital output of A/D converter for k^{\mbox{th}} photo-diode when
          output of interface is corrupted with noise
          interger (l = 1, 2, ...)
          less than
          much less than
          less than or equal to
          natural logarithm
1n
          logarithm to the base of 10
10g10
          noise voltage added to output of A/D converter
Na
```

sample average of Na Na kth photo-diode noise current and its variance sample average of nu N_{I}, σ_{I}^{2} noise voltage added to output of interface and its variance sample average of N_T N_{M}, σ_{M}^{2} noise voltage added to output of multiplex and its variance $\overline{N_M}$ sample average of N_M S step size of A/D converter σ_n^2 variance of combined N_a , N_I , n_k noise terms $\sigma_{n\ell}^2$ variance of combined noise terms as a function of £ output of interface for kth photo-diode **V**_T(k) $V_{I}^{N}(k)$ V_T(k) corrupted with noise $\Delta V_T(k)$ incremental change in $V_{T}(k)$ quantization estimate of noise-free interface output for kth photo- $V_{Iq}(k)$ diode $V_{Iq}^{N}(k)$ quantization estimate of noisy interface output for kth photodiode $\overline{V_{Iq}^{N}(k)}$ sample average of $V_{Iq}^{N}(k)$ multiplex output for kth photo-diode V_m(k) $V_{m}^{N}(k)$ $V_{m}(k)$ corrupted with noise $V_{\mathbf{m}}^{\mathbf{N}}(\mathbf{k})$ sample average of $V_{m}^{N}(k)$

Voff

voltage offset

1.0 INTRODUCTION

The Coarse Optical Power Spectrum Estimator (COPSE) at Defence Research Establishment Ottawa consists of a coherent optical Fourier transform system, a 64 element solid state detector, electronic hardware and software run on a NOVA 1200 and a XEROX Sigma 9 computer (Fig. 1). The signals coming from the 64 photo-diodes in the detector are first multiplexed onto one line. The multiplexed signal is then amplified, biased and amplified again before it is sampled and digitized by an A/D converter. The samples are subsequently stored on magnetic tape.

The various components of the COPSE Data Acquisition System were discussed in depth in an earlier report [1]. Only a brief summary will be presented here. Instead, this report is a continuation of that earlier one. It contains a theoretical analysis of the effect that additive Gaussian noise has on the system.

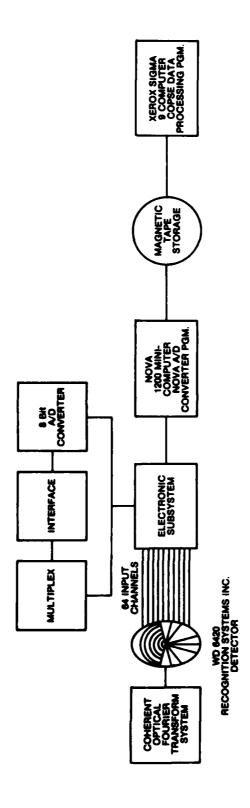


Fig. 1: COPSE System

2.0 COPSE DATA ACQUISITION SYSTEM

The data acquisition segment of the COPSE system consists of a 64 element solid state detector, electronic hardware, software and magnetic tape storage. The electronic hardware is further subdivided into three separate devices: a multiplex, an interface and an 8 bit A/D converter. The signals coming from the 64 photo-diodes of the detector are first switched onto one line by the multiplex. The multiplex allows for either linear or log mode of operation. Letting $i_{\bf k}$ and $V_{\bf m}({\bf k})$ represent the output current of the ${\bf k}^{\rm th}$ photo-diode and its corresponding multiplex output voltage respectively,

$$V_{m}(k) = -|i_{k}| \times 10^{4} \text{ volts}$$
 (1)

on linear mode provided

-15 nanoamps $< i_k < -1.3$ milliamps

and

$$V_{m}(k) = -10 - 2 \log_{10} |i_{k}|$$
 (2)

on log mode provided

-3 nanoamps $< i_k < -1$ milliamps.

 $|i_k|$ is the absolute value of i_k and k, the photo-diode element number, is an integer between 1 and 64.

The interface next biases and amplifies the multiplexed signal. The device gives the user the choice of several gains (G), scaling factors (M) and voltage offsets (Voff). The interface output voltage takes the form of

$$V_{I}(k) = -G[M V_{m}(k) + Voff] \text{ volts}$$
(3)

on linear mode and

$$V_{I}(k) = -G[V_{m}(k) + Voff -8] \text{ volts}$$
 (4)

on log mode when the input voltage is $V_m(k)$.

Substituting equation (1) in (3) and (2) in (4), and solving for $|i_k|$ in terms of $V_I(k)$,

$$\left|i_{k}\right| = \frac{V_{I}(k)}{GM} \times 10^{-4} + \frac{Voff}{M} \tag{5}$$

and

$$|i_k| = 10^{\frac{V_I(k)}{2G}} - 9 + \frac{Voff}{2}$$
 (6)

for the two modes. Hence, an incremental change in $\left|i_k\right|$ (Δ $\left|i_k\right|$) will result in a corresponding change in V $_I$ (k) of

$$\Delta V_{I}(k) = GM \times 10^{4} \Delta \left| i_{k} \right| \tag{7}$$

on linear and

$$\Delta V_{I}(k) = \frac{2G}{\ln 10} \frac{\Delta |i_{k}|}{|i_{k}|}$$
 (8)

on log. Linear mode gives a constant resolution throughout the photo-diode current range but, on the log mode, resolution depends on $|i_k|$. The two modes have the same resolution in situations where

$$\left| 1_{k} \right| = \frac{2 \times 10^{-4}}{10 \cdot 10} \cdot \frac{1}{M} \,. \tag{9}$$

Equations (7) and (8) are plotted in Figure 2.

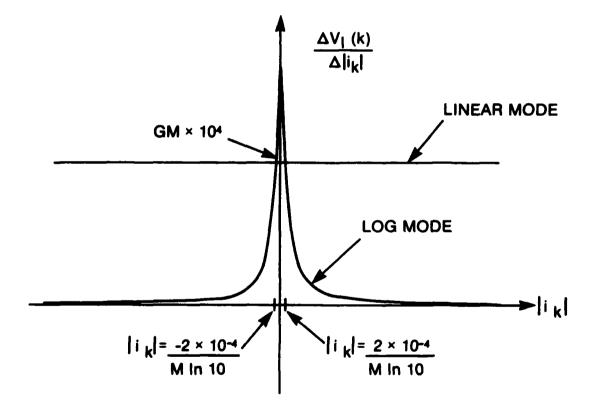


Fig. 2: Plot of $\frac{\Delta V_{I}(k)}{\Delta |i_{k}|}$ Versus $|i_{k}|$ for Both Modes of Operation

The A/D converter has an input voltage range of 0 to 10 volts. It converts $\mathbf{V}_{_{\mathbf{I}}}(\mathbf{k})$ into a binary number whose decimal equivalent $\mathbf{L}_{\mathbf{k}}$ satisfies

$$(L_k - 0.5)S < V_I(k) < (L_k + 0.5)S$$
 (10)

and is an integer between 0 and 255. The step size of the converter in the ${\tt COPSE}$ system

$$S = \frac{1}{25.6} . {11}$$

If the system is noise-free, the COPSE Data Processing program will approximate $\mathbf{V}_{\mathbf{I}}(\mathbf{k})$ by

$$V_{Iq}(k) = L_k S \tag{12}$$

with an error due to quantization of

$$e_{q} = V_{I}(k) - V_{Iq}(k). \tag{13}$$

Note, e_q varies between +0.5S and -0.5S.

The program calculates an estimate of $|i_k|$ ($|i_k|_p$) of

$$\left|i_{k}\right|_{e} = \left|i_{k}\right| - \frac{e_{q}}{GM} \times 10^{-4} \tag{14}$$

on linear mode and

$$\left|i_{k}\right|_{e} = \left|i_{k}\right| \ 10^{e_{q}/GM} \tag{15}$$

on log mode.

3.0 NOISE ANALYSIS

To include noise in the analysis, the COPSE Data Acquisition System is assumed to contain a series of strategically-placed current and voltage zero-mean, Gaussian noise generators. Referring to Figure 3, there is a current generator at the output of each of the 64 photo-diodes of the detector and voltage generators at the outputs of the three electronic devices. The noise terms are further assumed to be additive and statistically independent so equations (1) through (4) now take the form of

$$V_{M}^{N}(k) = -|i_{k}| \times 10^{4} + n_{k} \times 10^{4} + N_{M} \text{ volts}$$
 (16)

$$V_{M}^{N}(k) = -10 - \log_{10}(n_{K} + |i_{K}|) + N_{M} \text{ volts}$$
 (17)

$$V_{I}^{N}(k) = -G[M V_{M}^{N}(k) + Voff] + N_{T} \quad volts$$
 (18)

and

$$V_{I}^{N}(k) = -G[V_{M}^{N}(k) + Voff - 8] + N_{I} \quad volts$$
 (19)

where

 n_k, σ_k^2 the kth photo-diode noise current and its variance,

 N_{M} , σ_{M}^{2} noise voltage added to the output of the multiplex and its variance,

 N_{I}, σ_{I}^{2} noise voltage added to the output of the interface and its variance.

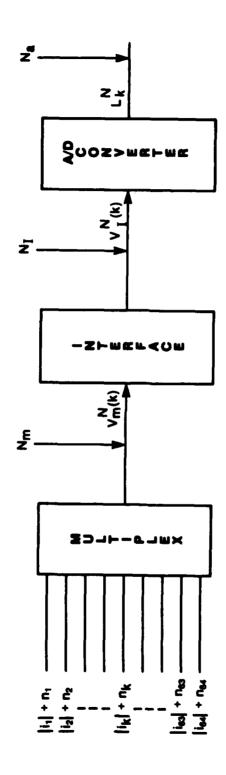


Fig. 3: COPSE Electronic Subsystem with Noise Added

The superscript N on $V_{I}^{N}(k)$ and on $V_{m}^{N}(k)$ denotes a signal which has been corrupted with noise.

The A/D converter converts $V_{L}^{N}\left(n\right)$ into a binary code whose decimal equivalent, represented now by $L_{k}^{N},$ must satisfy

$$(L_k^N - 0.5)S < v_I^N(k) < (L_k^N + 0.5)S.$$
 (20)

 $\mathsf{L}_{\mathsf{k}}^{\mathsf{N}}$ is an integer between 0 and 255. Hence, the error due to quantization is

$$e_{q}^{N} = V_{I}^{N}(k) - V_{Iq}^{N}(k)$$
 (21)

and

$$V_{Iq}^{N}(k) = L_{k}^{N}S. \qquad (22)$$

Before the digitized signal is processed, it is once more corrupted with added noise at the output of the interface.

$$L_k^N + L_k^N + N_a, \tag{23}$$

 N_a being the noise voltage.

The interface output for each photodiode is sampled and digitized 64 times. To average out the noise, the processing program calculates the averages of these samples and estimates $|i_k|$ to be:

$$|i_k|_e = |i_k| - \overline{n_k} - \overline{N_M} \times \frac{10^{-4}}{GM} [\overline{N_I} - \overline{e_q^N} + \overline{N_aS}]$$
 (24)

on linear mode and

$$|i_k|_e = |i_k| 10$$
 $\frac{1}{2G} (N_a S + N_I - e_q^N) - \frac{N_M}{2} 10 10 10 |i_k|_e |i_k|$ (25)

on log mode.

$$n_k$$
, N_M , N_I , e_q^N , $log_{10}[1 + \frac{n_k}{|i_k|}]$ and N_a

are the corresponding sample averages of

$$n_k$$
, N_M , N_I , e_q^N , $log_{10}[1 + \frac{n_k}{|i_k|}]$ and N_a

respectively.

The results of an experiment done with the COPSE system are presented in Figure 4. The detected intensity distribution was that of a collimated Gaussian beam of spot size 16.7mm. Both modes of operation were employed. The shape of the curves are what one would expect from a Gaussian beam which is shifted with respect to the center of the detector.

3.1 Linear Mode of Operation

As the number of samples taken of $V_{\tilde{I}}^{N}(k)$ increases, the averages in (24) and (25) approach their ensemble or expectation values. The expectation value of a Gaussian, zero-mean, random variable is zero [2]. Equation 24 therefore reduces to

$$|i_n|_e = |i_n| - \frac{E\{e_q^N\}}{GM} \frac{10^{-4}}{GM}$$
, (26)

The notation E{ } stands for the operation of ensemble averaging. If all the samples of $V_{I}^{N}(k)$ are within the range of the converter, it can be easily proved that

$$e_q + 0.5S \le E\{V_{Iq}^N(k)\} - V_{Iq}(k) < e_q - 0.5S$$
 (27)

where

$$E\{V_{Iq}^{N}(k)\} - V_{Iq}(k) = e_{q} - E\{e_{q}^{N}\}.$$
 (28)

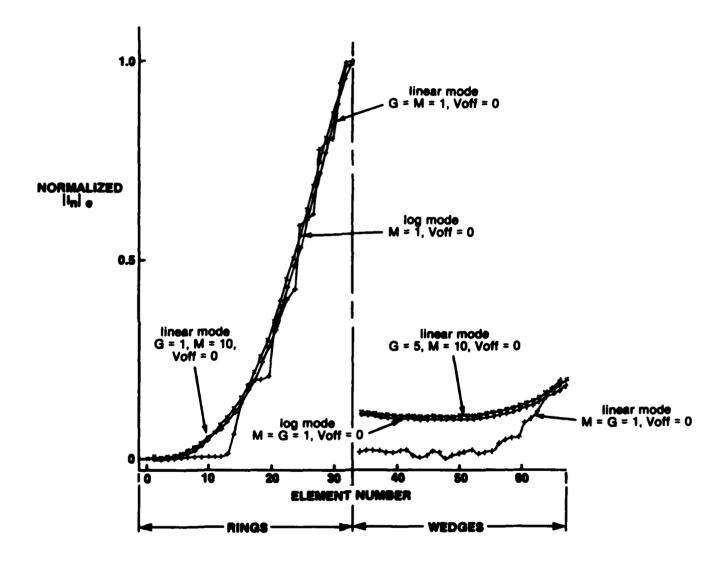


Fig. 4: Estimated Photo-Diode Output Currents for a Collimated Gaussian Beam (Spot Size of Collimated Beam = 16.7 mm)

 $E\{v_{Iq}^N\}$ has the same range of values as e_q ; i.e., $\pm 0.5S$. Futhermore, the expectation value of $V_{Iq}^N(k)$ is within one step size of its noise-free counterpart. In other words,

$$|E\{V_{Iq}^{N}(k)\} - V_{Iq}(k)| < S.$$
 (29)

A more rigorous discussion of the problem is contained in Korn's book [3]. Using his results and after some mathematical manipulation, it can be shown that $\mathsf{E}\{e_q^N\}$ is given by the sum of weighted sines:

$$E\{e_{q}^{N}\} = \frac{S}{\pi} \int_{\ell=1}^{\infty} \frac{(-1)^{\ell}}{\ell} \sin\left[\frac{\ell e_{q} 2\pi}{S}\right] \times \exp\left\{-\frac{2 \sigma_{n}^{2} \pi^{2} \ell^{2}}{S^{2}}\right\}, \quad (30)$$

Furthermore, since the noise terms are additive and statistically independent,

$$\sigma_n^2 = \sigma_1^2 + G^2 M^2 \times 10^8 \sigma_k^2 + G^2 M^2 \sigma_M^2$$
 (31)

Obviously, $E\{e_q^N\}$ depends on the step size of the converter, e_q and the noise statistics. The larger the ratio $\frac{\sigma_n}{S^2}$ is, the smaller $E\{e^N\}$ will be and the better the estimate of $|i_k|$ will be. Higher gains, scaling factors and noise variances will accomplish that. See Figure 5.

When

$$S \leq 3\sigma_{n}, \tag{32}$$

only the first term of the summation in (30) contributes appreciably to the estimate. Equation (30) can be approximated by

$$E\{e_q^N\} \cong \frac{S}{\pi} \sin \{\frac{2\pi e_q}{S}\} \exp \{\frac{-2\pi^2 \sigma_n^2}{S^2}\}.$$
 (33)

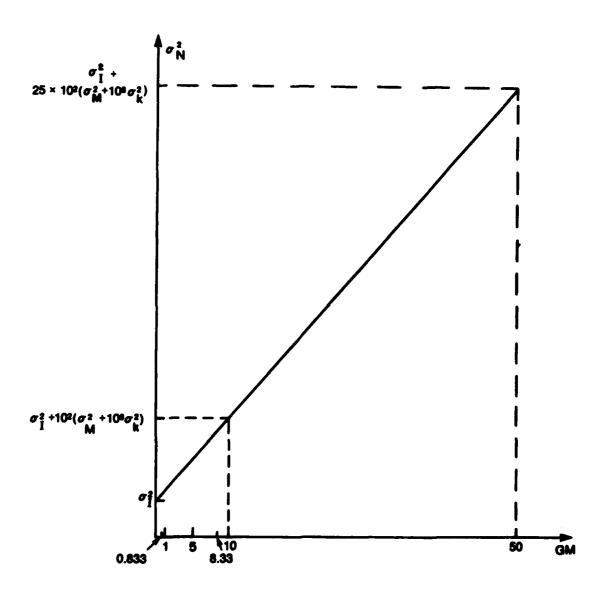


Fig. 5: Plot of σ_N^2 Versus G·M for Linear Mode of Operation (G = gain, M = scaling factor)

More terms must be included in the summation if S is larger or σ_n is smaller. Nevertheless, even when

$$S = 4\sigma_n, \tag{34}$$

 $E\{e_q^N\}$ is less than its corresponding noise-free value (Table 1). The noise tends to negate the effect of quantization provided the noise variance is high enough. In fact, in situations where e_q is zero or $\pm 0.5S$, it is theoretically possible to recover $|i_k|$ exactly.

Experiments done with the COPSE system indicate that $V_{Iq}^N(k)$ has a range of 1 to 6 step sizes depending on the element number. The higher ring elements, due to their larger areas, have noiser output currents.

It is a common practice in data processing schemes to correct for dark current. In the COPSE system, the correction can only be done when the system is on linear and there is no voltage offset. The correction was found to be insignificant.

3.2 Log Mode of Operation

Equation (25) becomes

in the limit as the number of samples taken of $Y_{\mathbf{I}}^{\mathbf{N}}(k)$ becomes large. Assuming that

$$-1 < \frac{n_k}{|i_k|} < 1, \tag{36}$$

which is a reasonable assumption to make,

 $\frac{\text{TABLE 1}}{\text{E}\{e_q^{\text{N}}\}\text{ ESTIMATES}}$

eq	S = σ _n	S = 20 _n	S = 3o _n	S = 40 _N
0	0	0	0	0
± S/16 (± 6.25 x 10 ⁻² S)	3.259 x 10 ⁻¹⁰ S	8.761 x 10 ⁻³ S	1.357 x 10 ⁻² \$	3.467 x 10 ⁻² S
± S/8 (± 1.25 x 10 ⁻¹ S)	6.022 x 10 ⁻¹⁰ \$	1.619 x 10 ⁻² S	2.508 x 10 ⁻² S	6.44 x 10 ⁻² S
± 3S/16 (± 1.875 x 10 ⁻¹ S)	7.868 x 10 ⁻¹⁰ S	2.115 x 10 ⁻² S	3.281 x 10 ⁻² S	8.483 x 10 ⁻² S
± S/4 (± 2.5 x 10 ⁻¹ S)	8.516 x 10 ⁻¹⁰ S	2.289 x 10 ⁻² S	3.551 x 10 ⁻² S	9.269 x 10 ⁻² S
± 5S/16 (± 3.125 x 10 ⁻¹ S)	7.868 x 10 ⁻¹⁰ S	2.115 x 10 ⁻² S	3.282 x 10 ⁻² S	8.645 x 10 ⁻² S
± 3S/8 (3.75 x 10 ⁻¹ S)	6.022 x 10 ⁻¹⁰ S	1.619 x 10 ⁻² S	2.513 x 10 ⁻² S	6.669 x 10 ⁻² S
± 7S/15 (±4.375 x 10 ⁻¹ S)	3.259 x 10 ⁻¹⁰ S	8.761 x 10 ⁻³ S	1.361 x 10 ⁻² S	3.628 x 10 ⁻² S
± S/2 (± 5 x 10 ⁻¹ S)	o	0	0	0
		<u> </u>		

the following approximation can be used:

$$\log_{10} \left(1 + \frac{n_k}{|i_k|}\right) \cong \frac{1}{\ln 10} \left[\frac{n_k}{|i_k|} - \frac{n_k^2}{2|i_k|^2} \right] \tag{37}$$

and, since n_k is a Gaussian, zero-mean, random variable, equation (35) becomes,

$$|i_{k}|_{e} = |i_{k}| \quad 10 \quad -\frac{E\{e_{q}^{N}\}}{2G} \quad -\frac{1}{2} \quad \frac{\sigma_{k}^{2}}{|i_{k}|^{2}} \quad \frac{1}{\ln 10} \quad . \tag{38}$$

 $|i_k|_e$ is not only limited by $E\{e_q^N\}$ but also by the statistics of the photodiode noise current and $|i_k|^2$. The lower the noise-free photo-diode current, the better will be the estimate of $|i_k|$. See Figure 4.

If all the samples of $V_{\rm I}^{\rm N}({\bf k})$ are within the range of the A/D converter,

$$-0.5S + \frac{G}{\ln 10} \frac{\sigma_k^2}{|i_k|^2} < V_I(k) - E\{V_{Iq}^N(k)\} < 0.5S + \frac{G}{\ln 10} \frac{\sigma_k^2}{|i_k|^2}. \quad (39)$$

Consequently, $E\{V_{Iq}^N(k)\}$ is within one step size of $V_{Iq}(k)$ even though its range of possible values are biased, i.e.,

$$-S + \frac{G}{\ln 10} \frac{\sigma_k^2}{|i_k|^2} < V_{Iq}(k) - E\{V_{Iq}^N(k)\} < S + \frac{G}{\ln 10} \frac{\sigma_k^2}{|i_k|^2}. \tag{40}$$

Again referring to Korn's book and after a great deal of mathematical manipulation, it was found that

$$E\{e_{q}^{N}\} = \frac{S}{\pi} \sum_{\ell=1}^{\infty} \frac{1}{(1 + \ell^{2}K^{2})^{\frac{1}{4}}} \exp\{\frac{-2\pi}{S^{2}} \ell^{2} \sigma_{n\ell}^{2}\} \times$$

$$\sin\{\frac{2\pi\ell}{S} e_{q} - \tan^{-1}(K\ell) + \frac{2}{S} \frac{G\pi\ell^{3}}{\ln 10} \frac{K}{1 + K^{2}\ell^{2}}\}$$
(41)

where

$$K = \frac{4G\pi}{S \ln 10} \frac{\sigma_k^2}{|f_k|^2}$$
 (42)

and

$$\sigma_{n\ell}^2 = G^2 \sigma_M^2 + \sigma_I^2 + \frac{4G^2}{\ln^2 10} \frac{\sigma_k^2}{|i_k|^2} \frac{1}{1 + K^2 \ell^2}$$
 (43)

 σ_{ne}^2 is plotted in Figure 6 as a function of $\frac{\sigma_k^2}{|i_k|^2}$ and £. Note, $\sigma_{n\ell}^2$ exhibits an exponential-like decay with £ and is a maximum at

$$\frac{\sigma_k^2}{|i_k|^2} = \frac{4G\pi\ell}{S \ln 10}. \tag{44}$$

Furthermore, since each term in the summation in (41) is multipled by a function that goes as the inverse of $\mathfrak{L}^2,$ one would not expect the higher terms in the summation to contribute significantly to $\mathsf{E}\{e_q^N\}.$

In the case of very weak photo-diode noise:

$$\frac{n_k^2}{|i_k|^2} \ll 1 , \qquad (45)$$

equation (41) reduces to a form similar to that of equation 33:

$$E\{e_q^N\} = \frac{S}{\pi} \sum_{\ell=1}^{\infty} \sin \left\{\frac{2\pi\ell}{S} e_q\right\} \exp \left\{\frac{-2\pi\ell^2}{S^2} \sigma_n^2\right\}$$
 (46)

and (see Figure 6)

$$\sigma_{n}^{2} = G^{2} \sigma_{M}^{2} + \sigma_{I}^{2} + \frac{4G^{2}}{\ln^{2} 10} \frac{\sigma_{k}^{2}}{\left|i_{k}\right|^{2}}.$$
 (47)

weak noise; slope = $4G^2/\ln^2 10$ $C_1 = \frac{16 \pi i}{S \ln^3 10} ; C_2 = \frac{256 \pi^4 i^4}{S^4 \ln^4 10}$ $G^2 \sigma_M^2 + \sigma_1^2$ $0 \frac{4G \pi i}{S \ln 10}$ σ_K^2

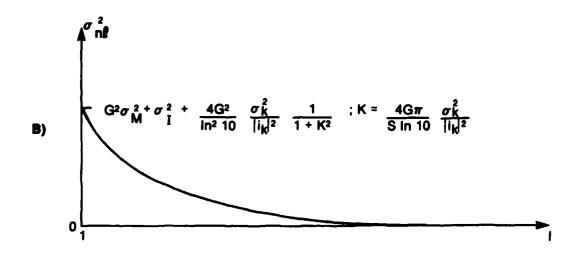


Fig. 6: A) Plot of $\sigma_{n\ell}^2$ Versus $\frac{\sigma_k^2}{|i_k|^2}$

B) Plot of $\sigma_{n\ell}^{\ 2}$ Versus ℓ on Log Mode

(S = step size of converter; G = gain; σ_M^2 , σ_I^2 , σ_k^2 = noise variances)

If eq is zero or $\pm 0.5S$, E{e_q^N} is zero but, according to equation 38, $\left|i_k\right|_e$ is not equal to $\left|i_k\right|$. It is

$$|i_{k}|_{e} \approx |i_{k}| 10^{-\frac{1}{2}} \frac{\sigma_{k}^{2}}{|i_{k}|^{2}} \frac{1}{\ln 10}$$
, (48)

The biasing effect of the log mode does not allow for this. Complete recovering of $\left|i_k\right|$ occurs only if

$$E\{e_q^N\} = \frac{-G}{\ln 10} \frac{\sigma_k^2}{|i_k|^2}$$
 (49)

Experiments done with the COPSE system on log mode indicated that $V_{1q}^N(k)$ has a range of values of 1 to 3 step sizes. The lower photo-diode currents have a wider range of sample values as expected.

4.0 REFERENCES

- 1. D.L. Desaulniers, C. Brochu, and F. Paquet. "A Data Acquisition System for a Coarse Optical Power Spectrum Estimator." <u>DREO</u> Technical Note 81-5.
- 2. A. Papoulis. <u>Probability, Random Variables and Stochastic</u> Processes. McGraw-Hill, Toronto, 1965.
- 3. G.A. Korn. Random-Process Simulation and Measurements. McGraw-Hill, Toronto, 1966.

UNCLASSIFIED

Security Classification

	DOCUMENT CONTROL DATA — R & D (Security classification of title, body of abstract and indexing annotation must be entered when the overall document is classified)				
1	ORIGINATING ACTIVITY DEFENCE RESEARCH ESTABLISHMENT OTTAWA	2a. DOCUMENT SECURITY CLASSIFICATION Unclassified			
	Department of National Defence		2b GROUP		
	Ottawa, Ontario, KlA 024, Canada				
3	DOCUMENT TITLE				
	NOISE ANALYSIS OF THE COARSE OPTICAL POWER SPECTRUM ESTIMATOR (COPSE) DATA ACQUISITION SYSTEM				
4	DESCRIPTIVE NOTES (Type of report and inclusive dates) Technical Note				
r,	AUTHOR(S) (Last name, first name, middle initial)				
	Desaulniers, D.L.				
6	DOCUMENT DATE March 1984	7a. TOTAL NO OF PAGES 7b. NO. OF REFS			
8a.	PROJECT, OR GRANT NO	9a ORIGINATOR'S DOCUMENT NUMBER(S)			
	33D00 °	DREO TN 82-8			
8ь	CONTRACT NO	9b. OTHER DOCUMENT NO.(S) (Any other numbers that may be assigned this document)			
10.	DISTRIBUTION STATEMENT				
	Unlimited				
11	SUPPLEMENTARY NOTES	12. SPONSORI	NG ACTIVITY		
		DREO			
1.3	ABSTRACT			-	

The various components of the COPSE Acquisition System are briefly summarized. The system is theoretically analysed to determine what effect added Gaussian noise will have on its performance. On linear mode, the Gaussian noise was found to negate the quantization effect of the system provided the variance of the noise was high enough. On log mode, the system was found to perform better in the low photo-diode current range.

UNCLASSIFIED

Security Classification

KEY WORDS

Gaussian noise

Analysis

Quantization

Linear mode

Log mode

Sample averaging

A/D converter

C.O.P.S.E.

Data acquisition

INSTRUCTIONS

- ORIGINATING ACTIVITY. Enter the name and address of the organization issuing the document.
- DOCUMENT SECURITY CLASSIFICATION: Enter the overall security classification of the document including special warning terms whenever applicable.
- 2b. GROUP: Enter security reclassification group number. The three groups are defined in Appendix 'M' of the DRB Security Regulations.
- DOCUMENT TITLE: Enter the complete document title in all capital letters. Titles in all cases should be unclassified. If a sufficiently descriptive title cannot be selected without classification, show title classification with the usual one-capital-letter abbreviation in parentheses immediately following the title.
- 4. DESCRIPTIVE NOTES: Enter the category of document, e.g. technical report, technical note or technical letter. If appropriate, enter the type of document, e.g. interim, progress, summary, annual or final. Give the inclusive dates when a specific reporting period is covered.
- AUTHOR(S): Enter the name(s) of author(s) as shown on or in the document. Enter last name, first name, middle initial.
 If military, show rank. The name of the principal author is an absolute minimum requirement.
- DOCUMENT DATE: Enter the date (month, year) of Establishment approval for publication of the document.
- TOTAL NUMBER OF PAGES. The total page count should follow normal pagination procedures, i.e., enter the number of pages containing information.
- 7b. NUMBER OF REFERENCES: Enter the total number of references cited in the document.
- 8e. PROJECT OR GRANT NUMBER: If appropriate, enter the applicable research and development project or grant number under which the document was written.
- 8b. CONTRACT NUMBER: If appropriate, enter the applicable number under which the document was written.
- 9a. ORIGINATOR'S DOCUMENT NUMBER(S) Enter the official document number by which the document will be identified and controlled by the originating activity. This number must be unique to this document.

- 9b. OTHER DOCUMENT NUMBER(S): If the document has been assigned any other document numbers (either by the originator or by the sponsor), also enter this number(s).
- 10. DISTRIBUTION STATEMENT: Enter any limitations on further dissemination of the document, other than those imposed by security classification, using standard statements such as:
 - (1) "Qualified requesters may obtain copies of this document from their defence documentation center."
 - (2) "Announcement and dissemination of this document is not authorized without prior approval from originating activity."
- 11. SUPPLEMENTARY NOTES: Use for additional explanatory notes
- SPONSORING ACTIVITY Enter the name of the departmental project office or laboratory sponsoring the research and development. Include address.
- 13. ABSTRACT: Enter an abstract giving a brief and factual summary of the document, even though it may also appear elsewhere in the body of the document itself. It is highly desirable that the abstract of classified documents be unclassified. Each paragraph of the abstract shall end with an indication of the security classification of the information in the paragraph (unless the document itself is unclassified) represented as (TS), (S), (C), (R), or (U).

The length of the abstract should be limited to 20 single-spaced standard typewritten lines, $7^{\rm to}$ inches long.

14. KEY WORDS. Key words are technically meaningful terms or short phrases that characterize a document and could be helpful in cataloging the document. Key words should be selected so that no security classification is required. Identifiers, such as equipment model designation, trade name, military project code name, geographic location, may be used as key words but will be followed by an indication of technical context.

END

FILMED

10-84

DTIC